

Syllabus

Math 01.331 - Introduction to Real Analysis II

COURSE DESCRIPTION:

Math 01.331 Introduction to Real Analysis II, 3 s.h.

Prerequisite: Math 01.330 (Introduction to Real Analysis I) with a grade of C- or better

This course is a continuation of Introduction to Real Analysis I. The purpose is to extend the student's understanding of basic analysis and the calculus. Topics included are: the mean-value theorem, existence of the Riemann integral, Riemann-Stieltjes integration, infinite series, convergence tests and Fourier series.

OBJECTIVE:

Students will demonstrate the ability to use rigorous mathematical thought processes in the following areas: sets, functions, sequences and series, limits, continuity, derivatives, integrals and Fourier series.

CONTENTS:

1.0 Mean Value Theorems

- 1.1 Local Maxima and Minima
- 1.2 Mean Value Theorem
- 1.3 Taylor's Theorem

2.0 Riemann Integral

- 2.1 Basic definition
- 2.2 Proof of the existence of the integral
- 2.3 Fundamental theorem of calculus
- 2.4 Properties of the integral
- 2.5 Improper integrals

3.0 Riemann-Stieltjes Integrals

- 3.1 Bounded version
- 3.2 Basic Theorems

4.0 Infinite Series

- 4.1 Definitions
- 4.2 Tests for convergence
- 4.3 Taylor Series

5.0 Sequences and Series of Functions

- 5.1 Definitions
- 5.2 Pointwise and uniform convergence
- 5.3 Uniform convergence of power series

6.0 Fourier Series

- 6.1 Convergence problems
- 6.2 Summability of Fourier series
- 6.3 Convergence of Fourier series
- 6.4 Orthogonal expansions

TEXT:

Generally, the same text is used in Introduction to Real Analysis II as was used in Introduction to Real Analysis I.

Edited: 04/2021